



## Figuring Percents A Lesson for Seventh and Eighth Graders

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*In Writing in Math Class: A Resource for Grades 2–8 (Math Solutions Publications, 1995), Marilyn Burns presents an activity Cathy Humphreys taught in her seventh- and eighth-grade math class. The students were learning about percents, and Cathy wanted to assess their ability to use percents in a problem-solving situation. She presented them with a problem created by Lynne Alper.*

Cathy wrote the following problem on the board:

*A school has 500 students. If a school bus holds 75 students, is there enough room on one bus for all of the school's left-handed students?*

Cathy first had the students report on a class graph whether they were right-handed or left-handed. They analyzed the data and compared them to the information Cathy had researched that 12 to 12 1/2 percent of Americans are left-handed. The students then tackled the problem, working in pairs. Listening as partners discussed the problem provided Cathy with some information about the students' perceptions. Reading the students' solutions contributed further to Cathy's assessment of their understanding and confusion.

Several pairs of students multiplied to solve the problem. Liz and Audry wrote: *To get the answer we multiplied 500 students by 12% and got 60 people and the bus can hold 75 people so there is enough room.*

Joey and Tony multiplied  $12.5 \times 5$  and got 62.5. They rounded this up to 63 and wrote: *Yes, because there are 63 students that are left handed.*

Other students used different reasoning processes. Marshay and Kiet wrote: *Yes, there are enough seats to hold all of the left handed people because 10% of 500 is 50 people, 2% of 500 is 10 people, so  $50 + 10$  is 60 people, and each bus hold 75 people.*

Eric and James wrote: *Yes, there are enough seats on the bus to fit the left-handed children. There are 63 left handed kids. We got the answer by using part of our homework. 10% of 500 is 50. 5% of 500 is 25—this was halved.*

Khalil and Gina took a different approach: *We think you can because 75 is 15% of 500. We only have to put 12% on of the left handed people.*

Right answers alone can hide a lack of understanding. No matter the method they chose, all of the students arrived at the correct answer that there was enough room for all the left-handed students. If the students had reported only answers, Cathy might not have learned about some of the students' confusion. Their written responses served to alert Cathy to some conceptual misunderstandings.

For example, some groups tried using division. Jon and Phil divided 12 into 500 and wrote: *After we did the problem we got 41.66 and it kept going on so we rounded it off to 42 students. We then*

subtracted 75 into 42 and got 33. After we got 33 seats we knew all the left handed people could get on the bus. (See Figure 1.)

SCHOOL BUS PROBLEM

$$\begin{array}{r}
 41.66 \\
 12 \overline{) 500.00} \\
 \underline{48} \phantom{00} \\
 20 \phantom{00} \\
 \underline{12} \phantom{00} \\
 80 \phantom{00} \\
 \underline{72} \phantom{00} \\
 80
 \end{array}$$

After we did the problem we got 41.66 and it kept on going so we rounded it off to 42 students. We then subtracted 75 into 42 and got:

$$\begin{array}{r}
 75 \\
 42 \\
 \hline
 33
 \end{array}$$

After we got 33 seats we knew all the left handed people could get on the bus.

Figure 1. Jon and Phil did not understand how to solve the problem.

Raymond, Paula, and Stephanie also used division, but they divided 500 into 12. They wrote: yes,  $12 \div 500 = 0.024$  ( $12\% \div 500$ ) so out of 500 students 24 of them are left handed so the bus can hold all the left handed people. (See Figure 2.)

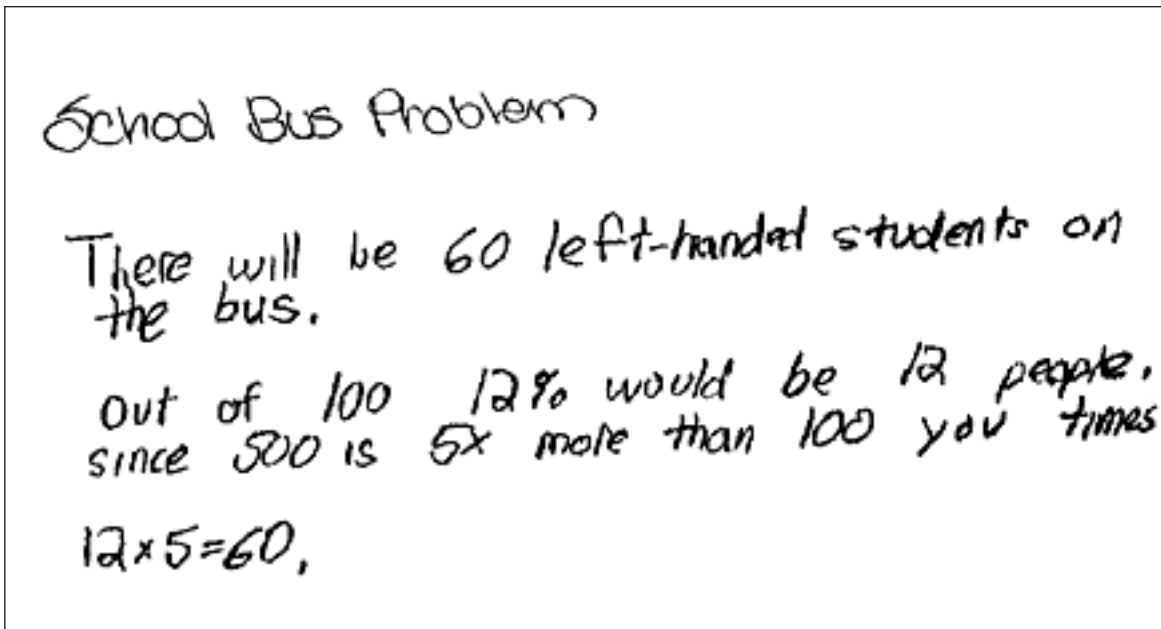


Figure 2. Raymond, Paula, and Stephanie came to the right conclusion, but their paper revealed their lack of understanding.

Cathy followed this assessment with an individual writing assignment titled “What I Know About Percents (So Far).” She told the students that their writing would help her learn what they understood and therefore help her plan more effectively for their continued learning. A writing assignment such as this gives value to students’ thoughts and involves students in reflecting on their own learning processes.

“Should we tell how we solve problems?” Nam asked.

“If that will give me information about your thinking and understanding, then it would be helpful,” Cathy answered. “The more information you give, the better.”

In their papers, the students included information about what percents are, situations in which percents are used, and ways to represent percents. Darshana, for example, wrote: *I know that percent is used for many things. It is used for grading, weather, tipping, and surveying. I learned how to estimate more accurately. I also learned that 100 is the main factor in percents. That means a pie is 100% or, 2% means .02 hundredths. Fractions are related to percents. That means 1/2 is also 50%. Some good ways to figure out percents are paper and pencil, calculators, and your mind.*

An issue that appeared in several students’ papers was how large percents can be. Nam, for example, began his paper with *I know that the maximum percent is 100.* Jena, however, began her paper with *I know that if there were 100 dollars each would count for 1%. Percent can go up to 100%, and sometimes over.*

Some students wrote about difficulties they were having. Tony included in his paper: *I know that \$25 is twenty-five percent out of \$100. I know that  $\frac{1}{4}$  is 20% out of 100%. I also know that percents are used everywhere and a lot of the time. Some problems that I have with percents are ones I don't understand. For example 13% out of \$15.00. Or 23 percent out of \$300.00. These problems and some problems like these are the ones I don't really understand. I guess the ones I don't understand are the ones that have an odd number for a percent.*

Stephanie wrote about her confusion: *So far all I know about percent is that it is very confusing! I think I understand how to solve a percent problem but since we didn't do percents last year this is my first time doing percents I am easily confused when a new way to solve a problem pops out at me. Here is an example of what I think when you ask what 20% means to me. Well if you take a dollar you know that there are 100 pennies in that dollar. And when you have that 100% that means that each penny stands for 1% so 20% of a dollar is 20 cents.*

From reading the students' papers, Cathy learned about the range of their understanding and their levels of confidence. The papers also provided some specific direction for further instruction. The references to the possible maximum size of percents were an indication that this issue needed attention in class. Also, the frequent mention of money was evidence of its usefulness for helping students think about percents.