

Lisa Rogers

# Visual Tools:

## When, Where and How to Help Students Achieve Number Sense



# @clakar #math\_solutions

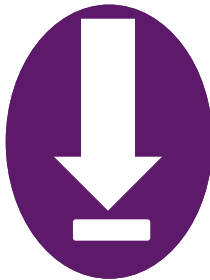


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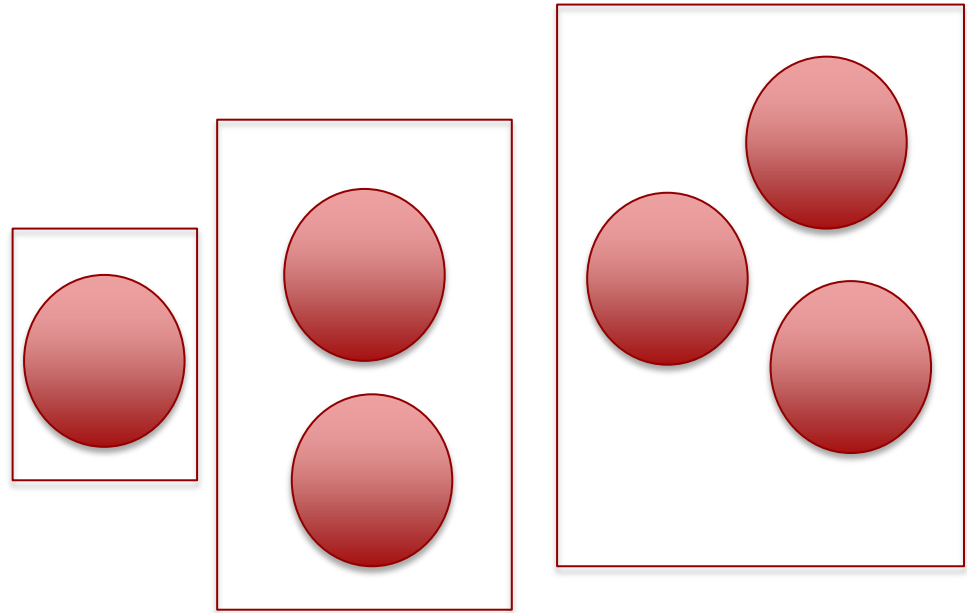
# Subitizing

- ***What is Subitizing?*** (Turn and talk)
- The term is derived from the Latin adjective **subitus** (meaning "sudden") and captures a feeling of immediately knowing how many items lie within the visual scene
- **“instantly seeing how many”**

# Rational- lays the groundwork for operations

- Quick images give students experience counting and seeing (*subitizing*) numbers.
- Students can make connections between how they see the dots and the possible symbolic equations.
- 2 phases of Subitizing:
  - **Perceptual subitizing**- ability to see a group and know how many without counting
  - **Conceptual subitizing**- ability to see more than one group and add them together to find the total.

# Subitizing Research



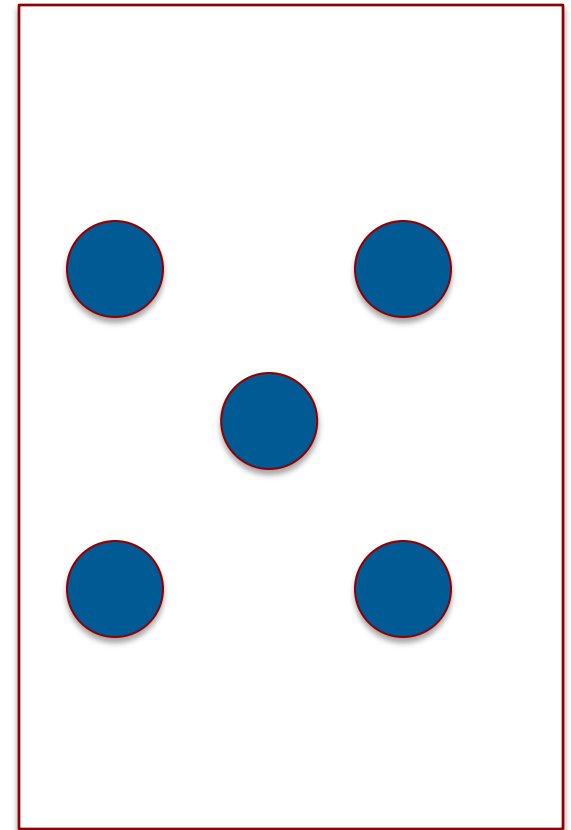
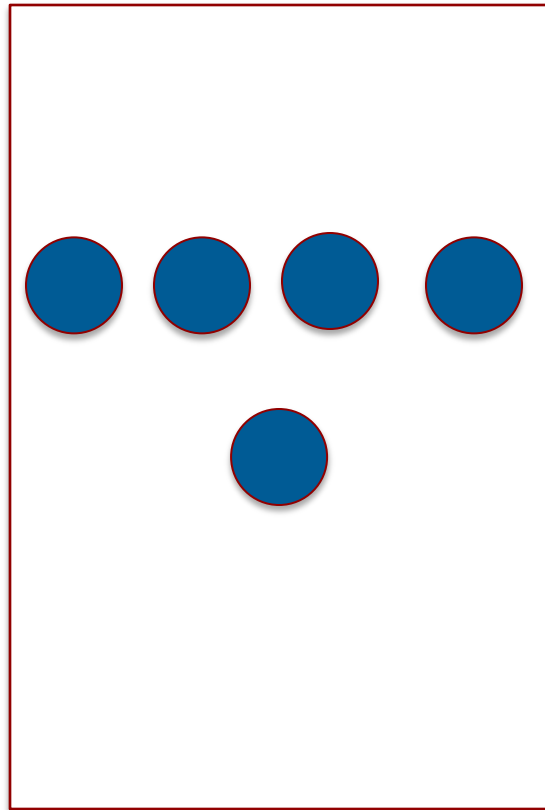
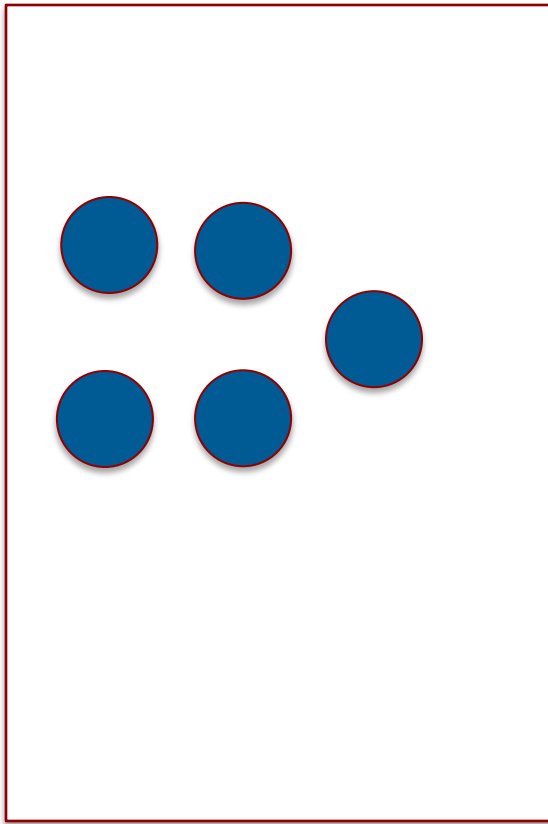
# Number Strings

A collection of purposefully chosen computation problems that build on one another to support students' mathematical thinking.

*Note: The problems within each string should be presented in sequential order.*

# Number String Example

## Kindergarten





**What did you see?**

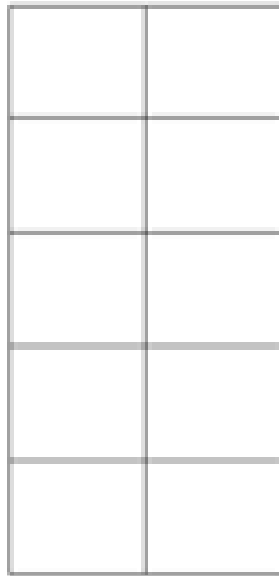
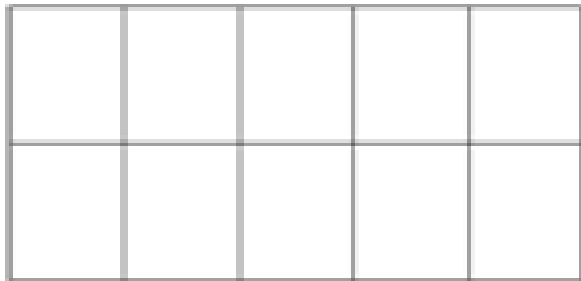
**How did you see it?**

# Dot Arrangements

# Subitizing Supports

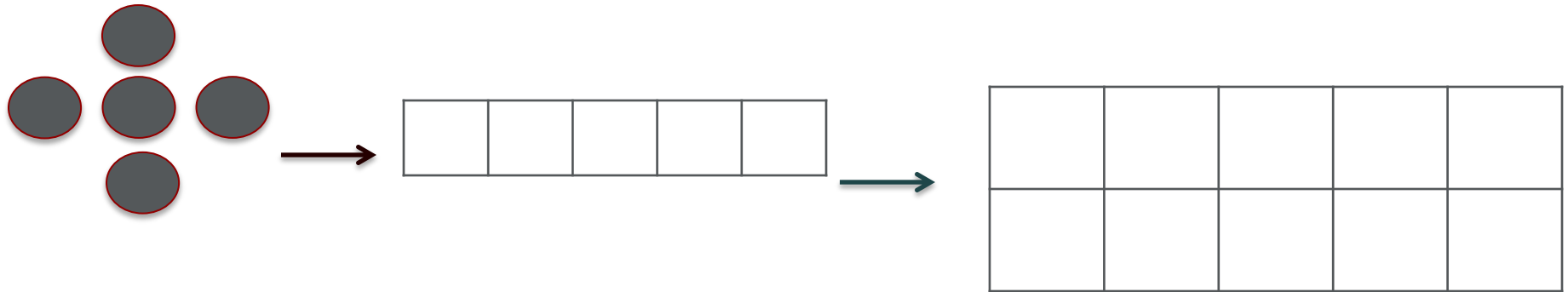
- Counting on strategies
- Development of conservation of number
- Learning basic facts
- Decomposing numbers
- Development of addition strategies
- Development of multiplication strategies
- Understanding of equality

# Ten Frames

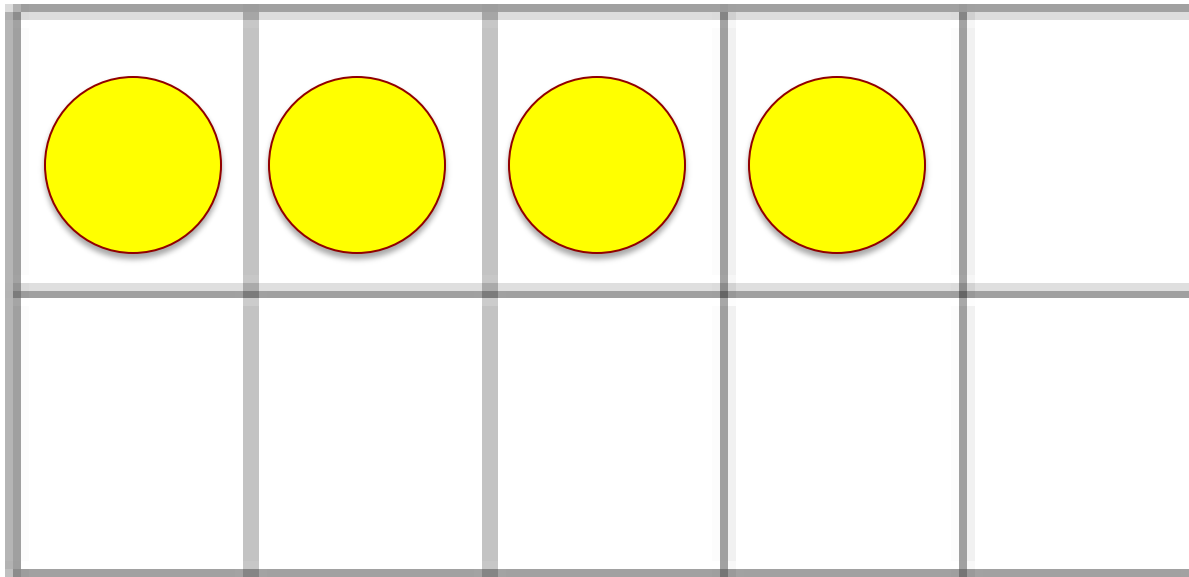


- Deepens the understanding of landmark numbers; 5 and 10
- Develops the ability to use landmark numbers
- Develops computational fluency

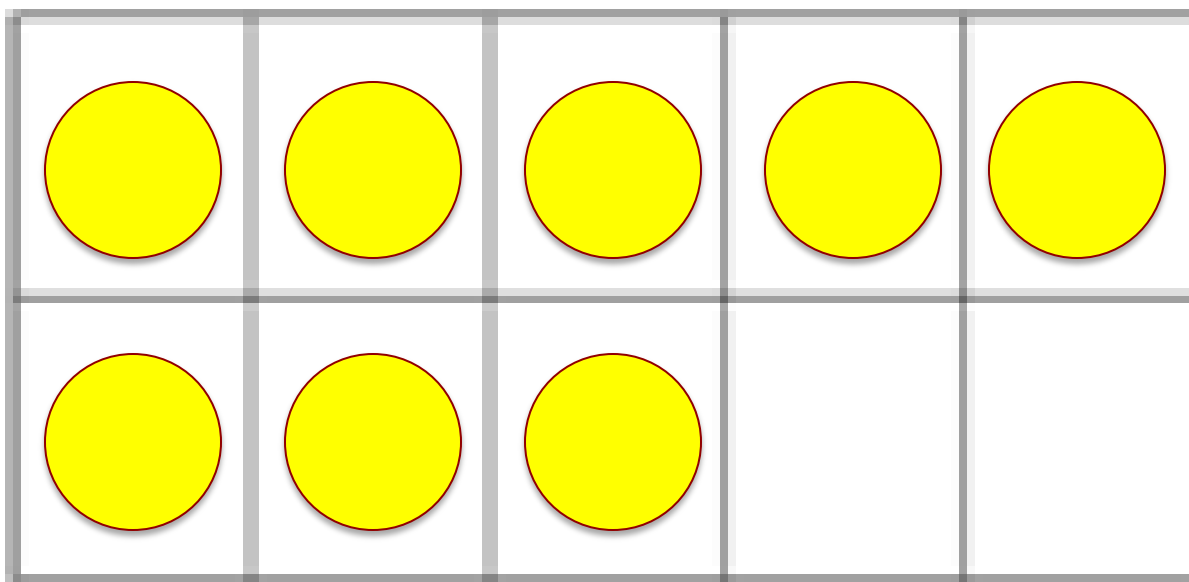
# Progression



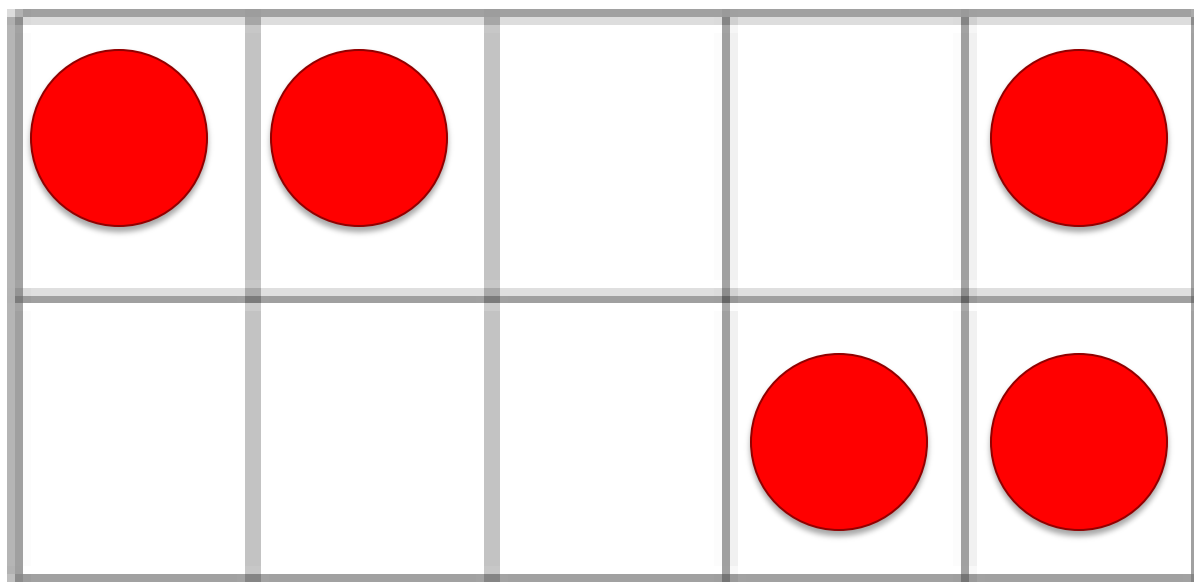
**How many dots are in the ten—frame?  
How did you figure it out?**



**How many dots are in the ten—frame?  
How did you figure it out?**



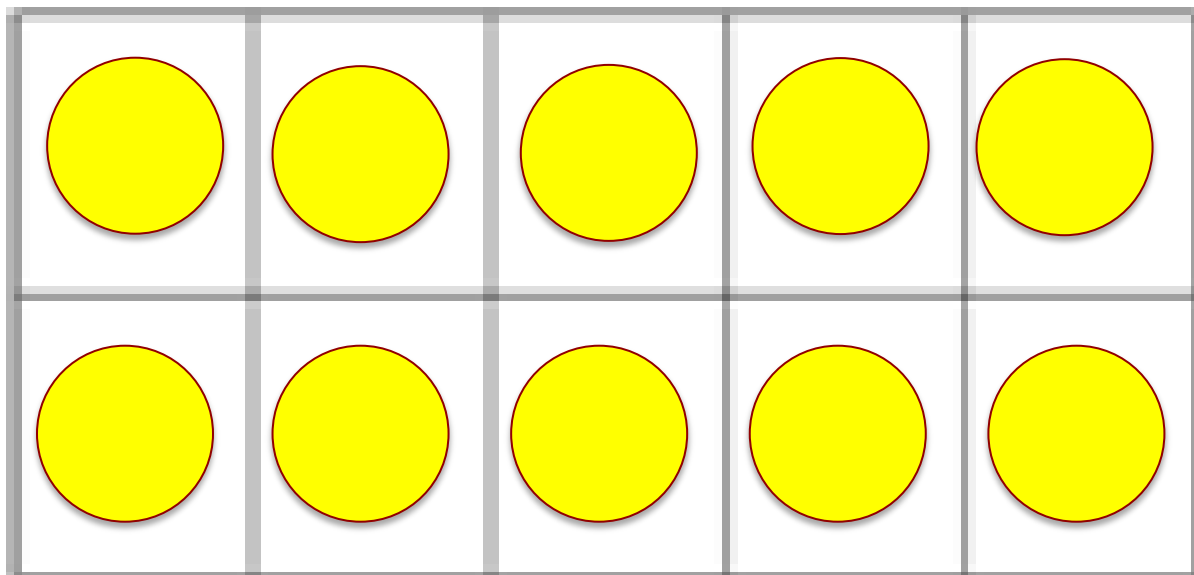
# Build what you see.





# Riddles Using a Double Ten—Frame

- My double ten—frame has more than 8 counters.
- My double ten—frame has fewer than 17 counters.
- My double ten—frame has a number of counters you say when you skip count by threes.
- My double ten—frame has 3 rows of five counters.



More than 8?

$$15 > 8$$

Fewer than 17?

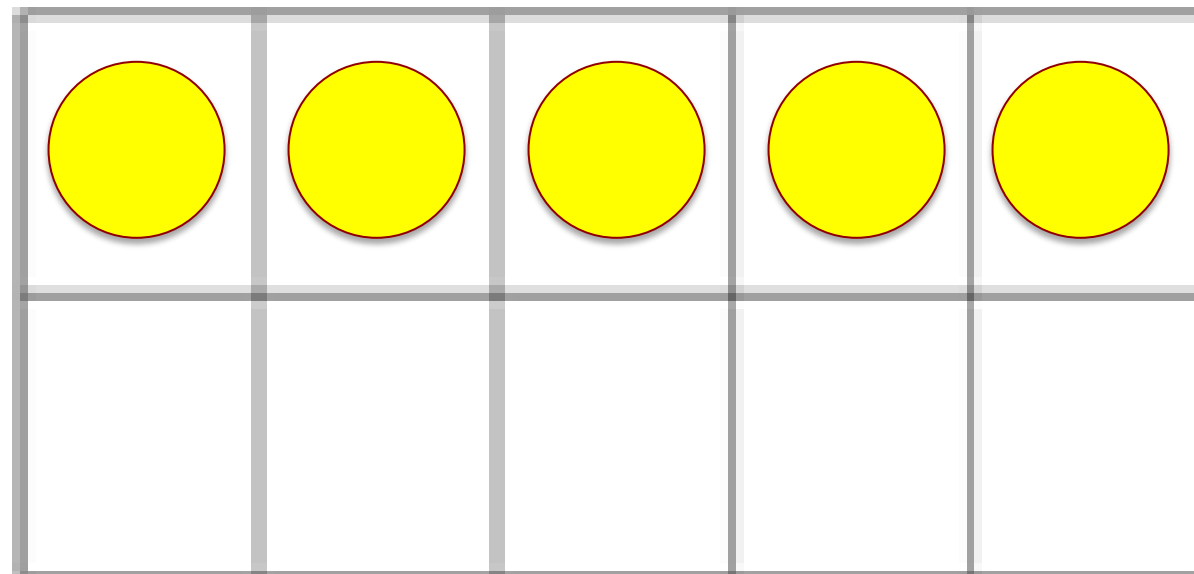
$$15 < 17$$

Skip count by 3s?

3, 6, 9, 12, 15

3 rows of 5?

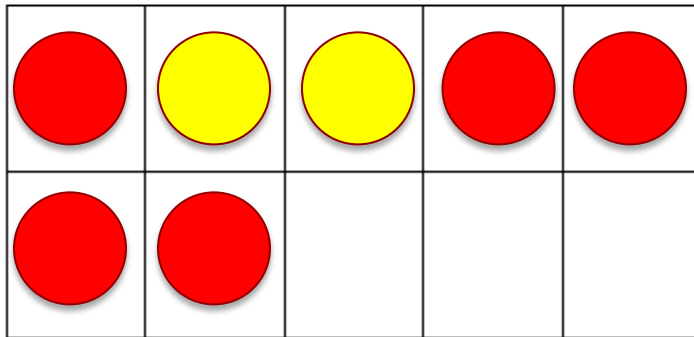
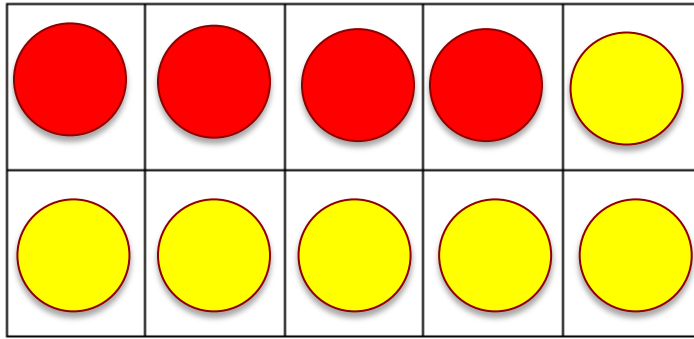
$$5 + 5 + 5$$



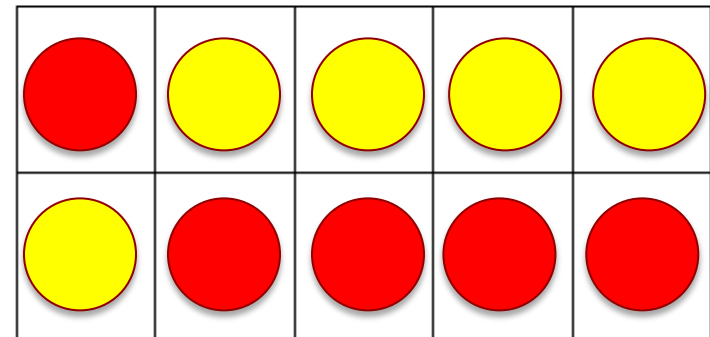
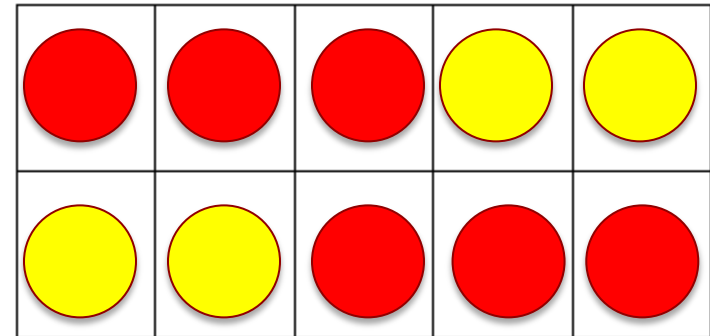
# Riddles

- Pick a number 1—10.
- Write a comparison statement.
- Write a comparison statement using the opposite phrase as the one used in the first clue.
- Write a clue referring to a skill you want the class to work on.
- Write a clue incorporating an arithmetic calculation to reveal the amount.

# Race for 20



$$4 + 6 + 1 + 2 + 4$$



$$3 + 4 + 4 + 5 + 4$$

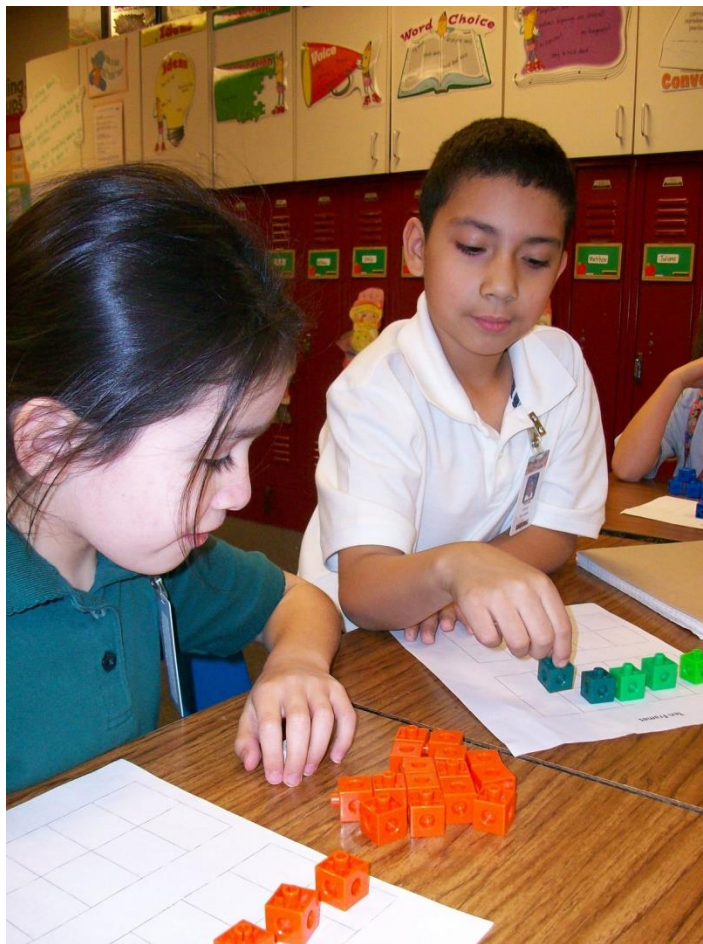
# Race to 20

- Decide who will go first.
- Roll the die.
- Using two color counters, mark the amount you rolled. Remember to switch colors each round.
- Play until someone reaches or goes over 20.
- Practice asking questions as you play.
- Record your number sentences.

# Possible key questions

- How many do you need to fill the ten frame (or both ten frames)?
- How would that look in a number sentence? (Ex  $4 + \underline{\quad} = 10$ )
- Who has more, how many more?
- What do you hope to roll and why?

# Options for the Game



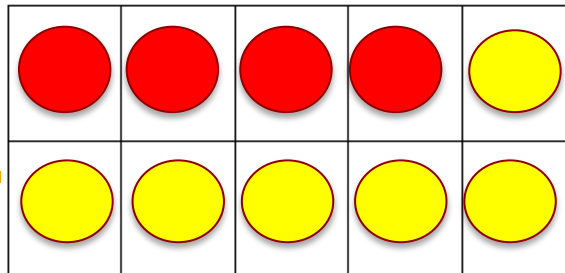
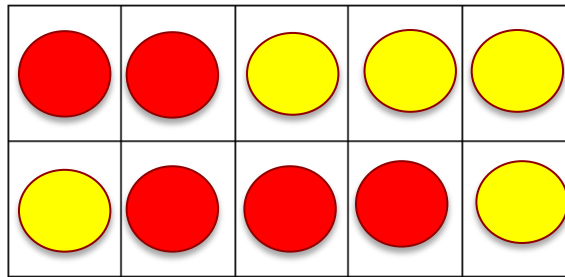
- Cover the 6 with a small sticker. Have students answer a key question when they roll the side with the sticker.
- Race for 10 (dice 1,1,2,2,3,3)

# Assessing

Use previously played games to connect pictures to number sentences.

What number sentences match the game board?

How would you add these numbers together?



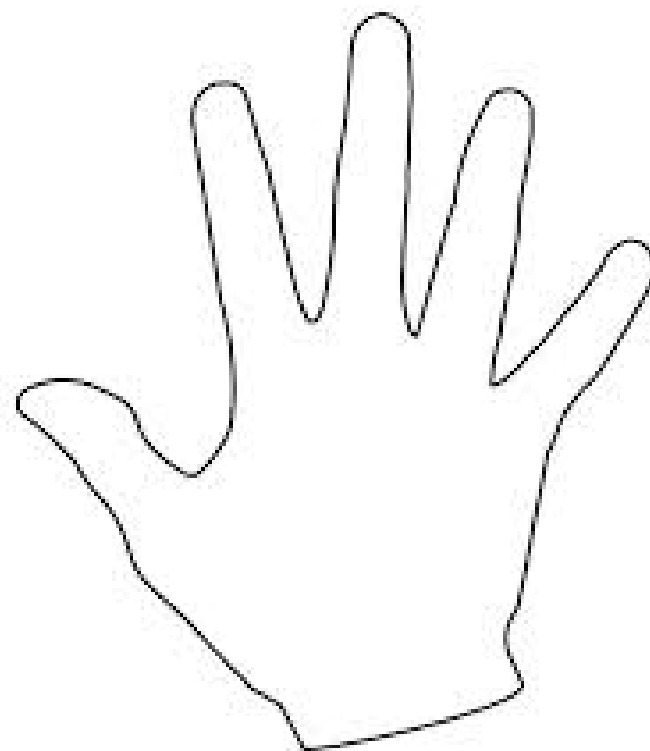
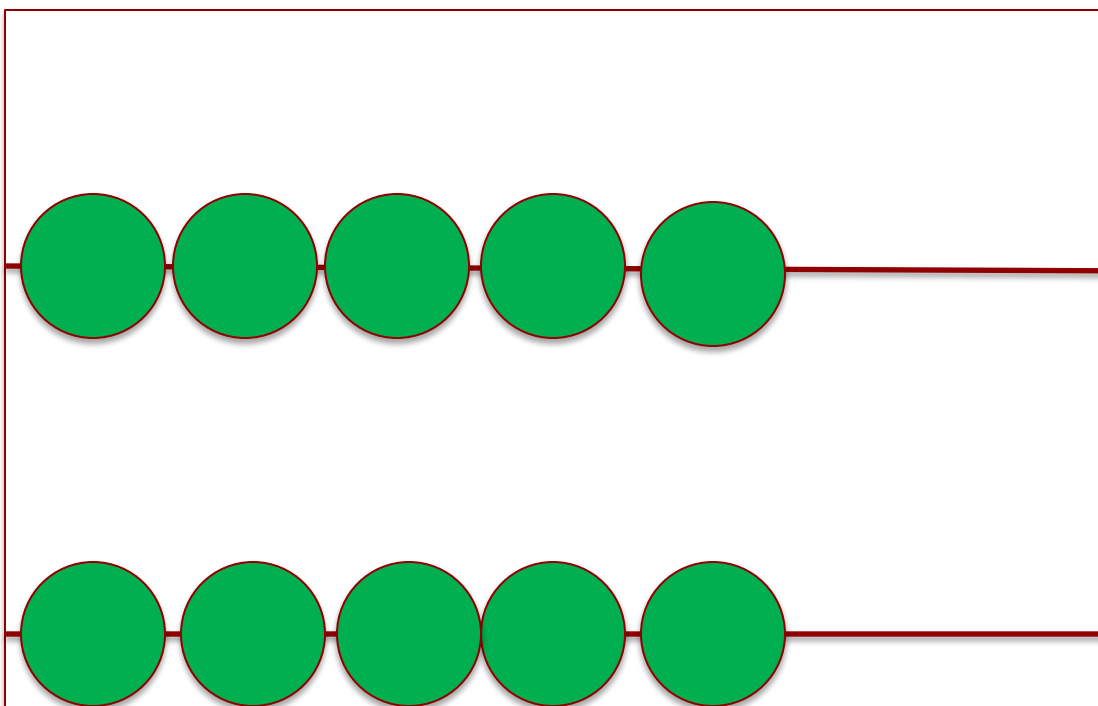


# Look Quick with Rekenreks

- How many dots do you see?
- How do you see them?



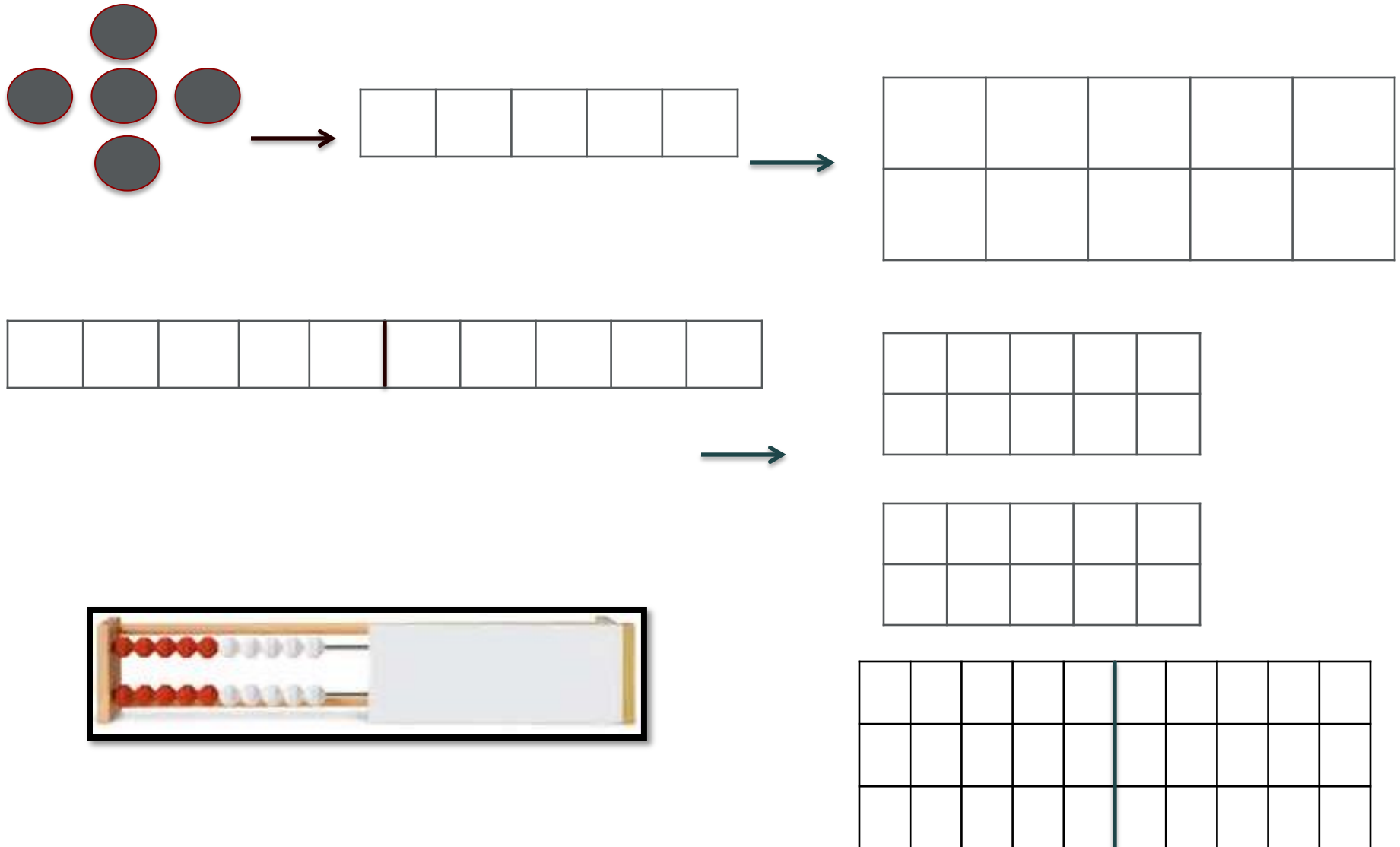
# Look Quick with Rekenreks



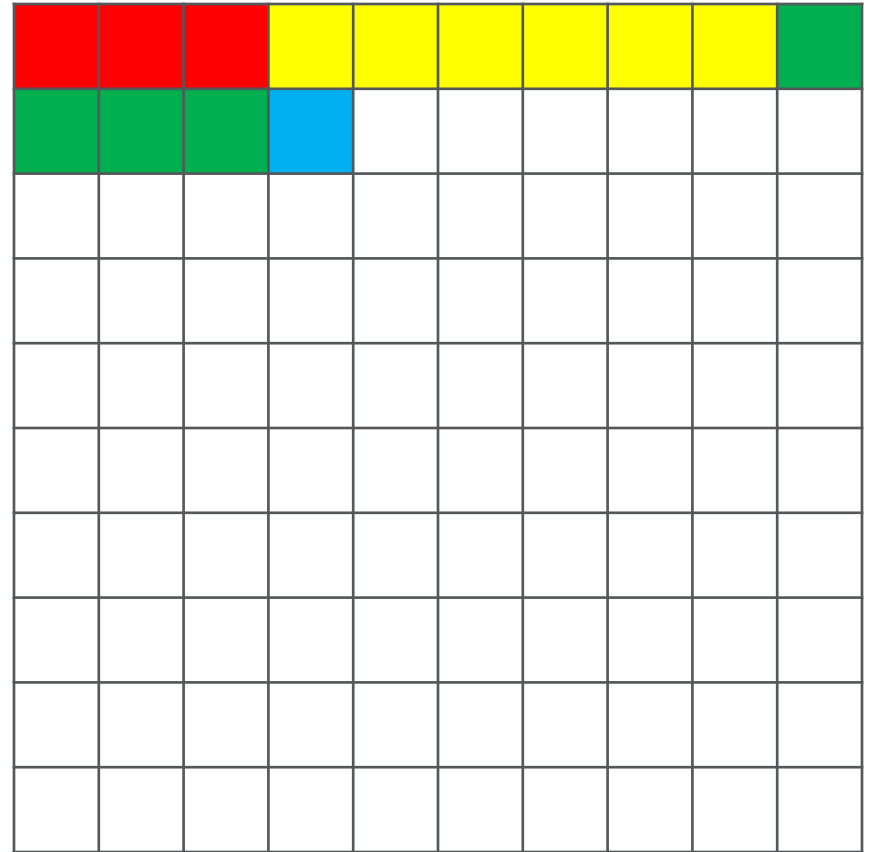
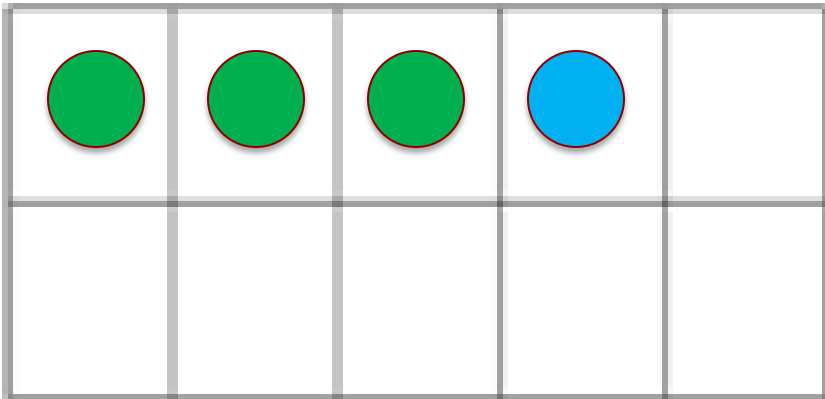
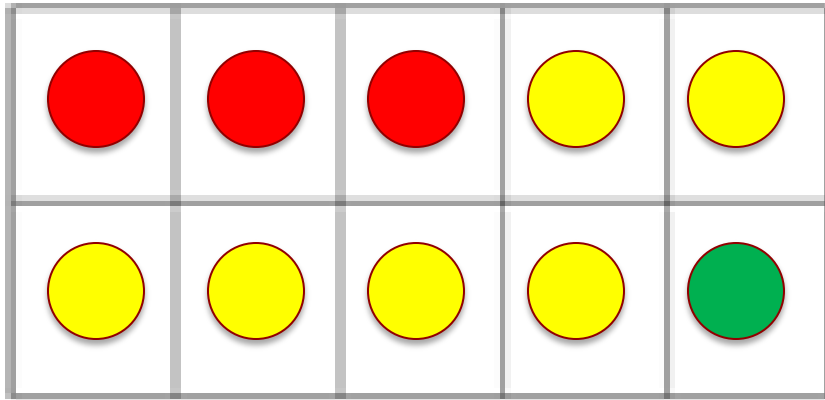
# Look Quick with Rekenreks

- How many dots do you see?
- How do you see them?

# Progression



$$14 = 3 + 6 + 4 + 1 \quad \text{or} \quad 14 = 10 + 4$$



# 1–100 Chart

Target Number!

+ or -

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

You can make hops of:

- Ones
- Tens
- Hundreds

# Hippity Hop

With a partner, investigate the following target numbers:

33

78

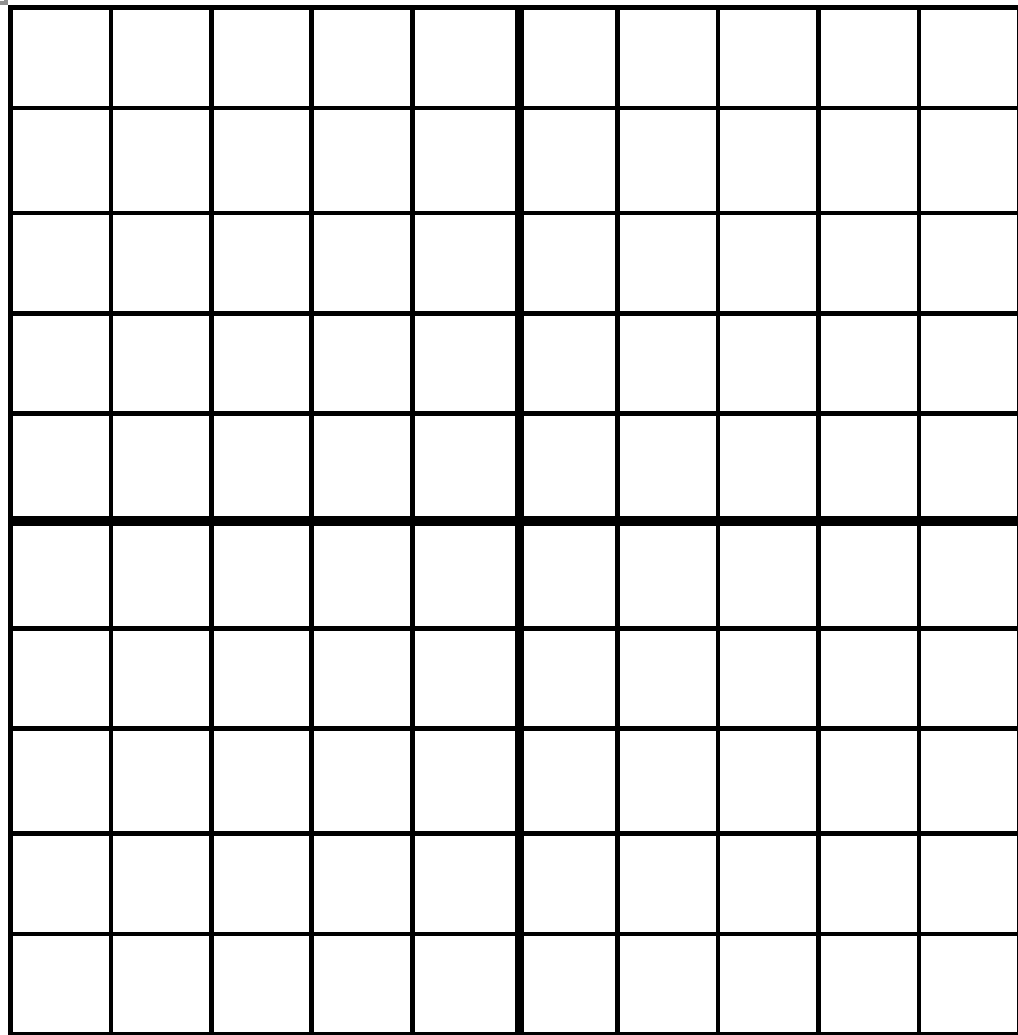
82

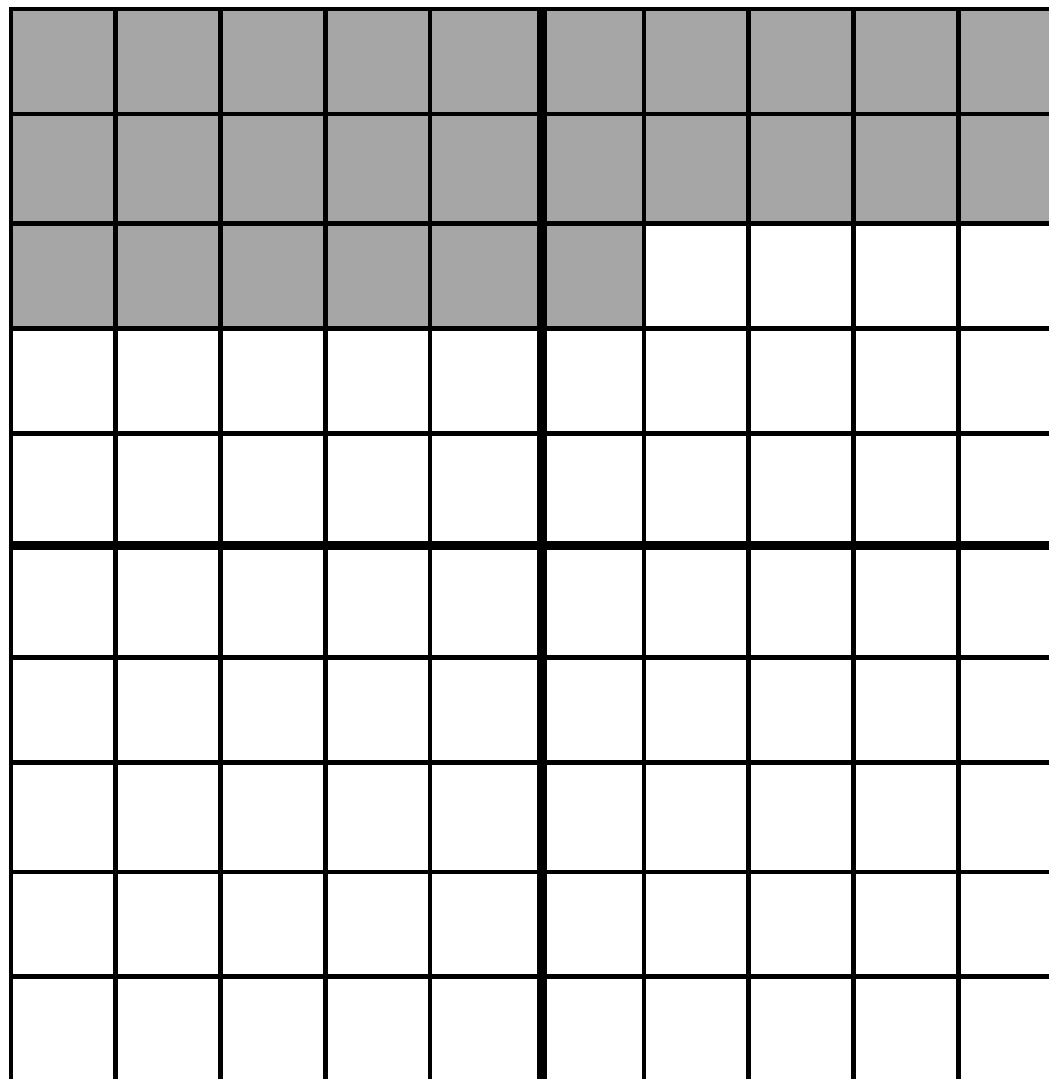
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

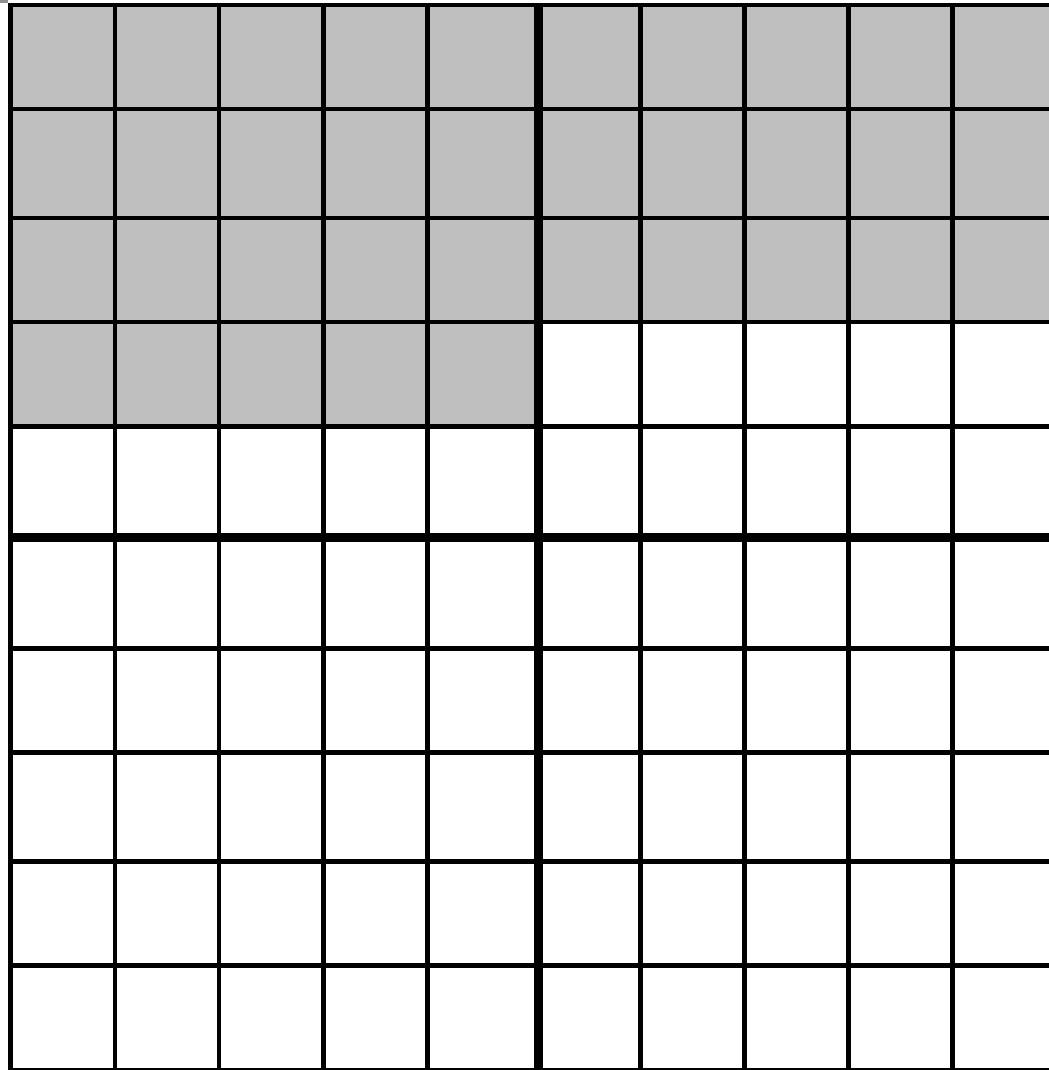
# Processing HIPPety Hop

- What's the value in requiring students to record an equation for each strategy doing this?
- How do you think your students would benefit from this routine?
- One way you can use this routine is as a lesson for an entire math class. What are other ways you could give students' opportunities to revisit it?









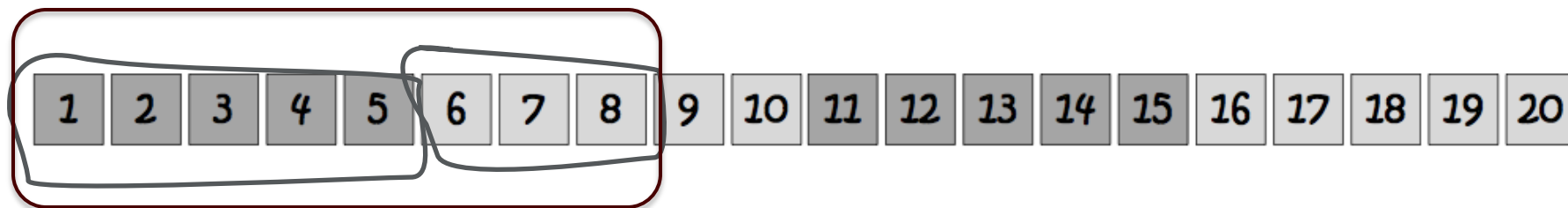
# Hundred Charts Help Students:

- Count
- Model addition and subtraction strategies
- Notice important ideas about our system of tens
- Solve problems once they are comfortable with its structure

# Number Lines and Number Paths



$$5 + 3 = 8$$



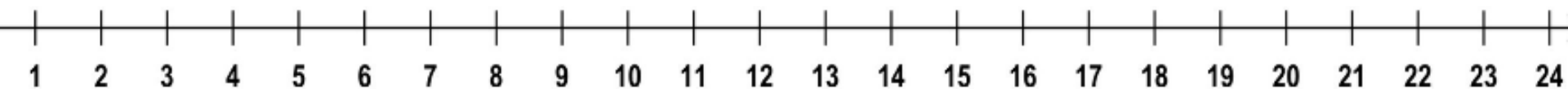
# Guess My Number



- My number is between \_\_\_\_ and \_\_\_\_\_. It's less than \_\_\_\_ and greater than \_\_\_\_\_.



# Guess My Number



The secret number is less than \_\_\_\_\_.

The secret number is greater than \_\_\_\_\_.

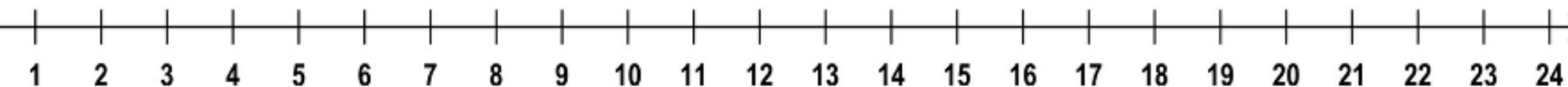
The secret number is between \_\_\_\_\_ and \_\_\_\_\_.

# Guess My Number





# Guess My Number



0

50

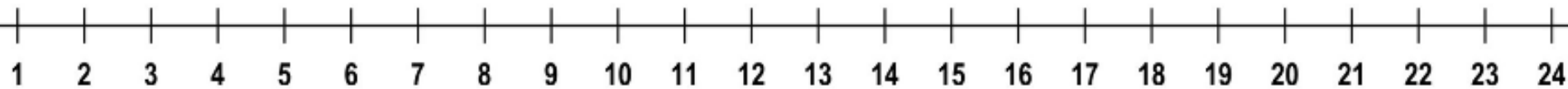
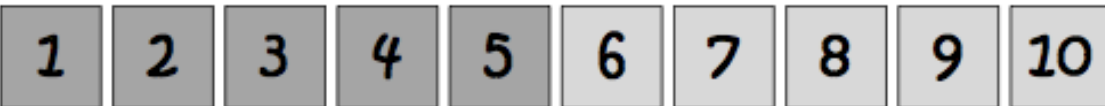
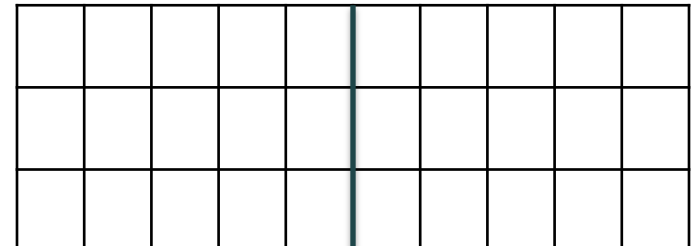
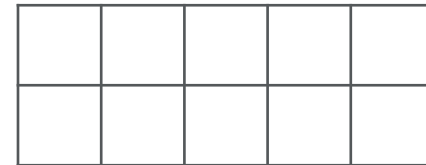
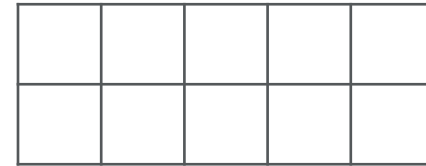
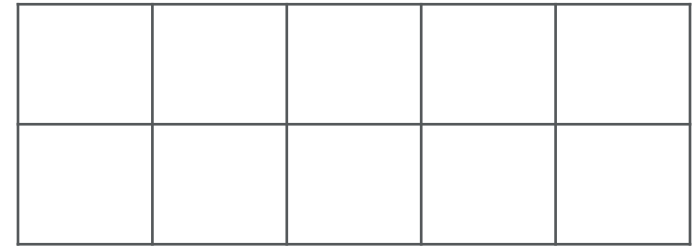
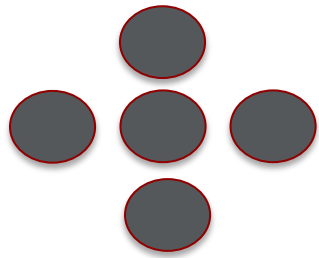
- You choose which version...
- Play in pairs: 2 rounds: each take a turn guessing

- The third version highlights the importance of benchmark numbers. Why are these important to think about?
- Do you think the number line is an effective tool for thinking about number relationships? Why or why not?

# Number Lines Help Students:

- Count
- Model addition and subtraction strategies
- Number Relationships (whole, integers, fractions, decimals)
- Solve problems once they are comfortable with its structure
- Explore Measurement

# Progression



# Thank you!!!

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